

Sasin | **'Interest Risk Management with Var Preview'**

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Sasin | **Outline – The Big Picture**

Risk Introduction

1. Definition and Sources of Risk
2. Risk Management

- Evolution of Risk Management Technique
 1. Management of Earnings (1970's) :
 2. Management of Value (1980's) :
 3. Multi-dimensional Risk Management
 - a) Value at Risk (Var) – The Preview
 - The Key Concept and Issues
 - Historical /Simulation/Analytic Method
 - VAR Pro and Con
 - b) Asset Liability Management/Optimization

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Sasin | **Figure 1 : Drivers of unexpected outcomes**

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graph LR
    A[Unexpected outcomes] --> B[Uncertainty]
    A --> C[Risk]
    A --> D[Equivocality]
    A --> E[Error]
    F[Lack of information] --> B
    G[Lack of knowledge] --> C
    H[Lack of judgement] --> D
    I[Lack of care] --> E
  
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Sources of Risks

•What is (financial) risk ?

Risk is defined as the uncertainty of future outcomes which come primarily from three fundamental forces :

- 1) Product market (inherent) risk: Unsys. Rate Risk ?
- 2) Strategic Risk : Budget for Risk Appetite
- 3) **Financial (market) Risk : Sys. Int. Rate Risk**

Financial (market) risk associated with an economic undertaking is the possibility of suffering a significant economic loss in the future.

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Sources of Risks -(Cont.)

• Risk and Return – Ex Ante

The analysis of risk and return of fixed-income securities depends extensively on the concept of **discounting** and the concept of **time value of money**.

The key is to find an 'appropriate' discount rate for each and single period under uncertainty world.

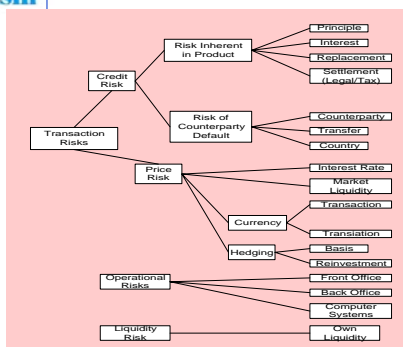
• Sources of Risk

Question : What are the risk factors for two years US government note to a Thai investor ?

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FIGURE 2 : Analysis of Risk Categories



Source :-Price Waterhouse : Financial Times Conference Organization , London 1992

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Risks Associated with Investing in Fixed Income Securities (a)

- Market, or Interest Rate Risk
- Reinvestment Risk
- Timing, or Call Risk Credit, or Default Risk
- Yield-curve, or maturity Risk
- Inflation, or purchasing power Risk
- Marketability, or Liquidity Risk

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Risks Associated with Investing in Fixed Income Securities (b)

- Exchange rate, or Currency Risk
- Volatility Risk
- Political or Legal Risk
- Event Risk
- Sector Risk
- Systemic/Correlation Risk
- Model Risk

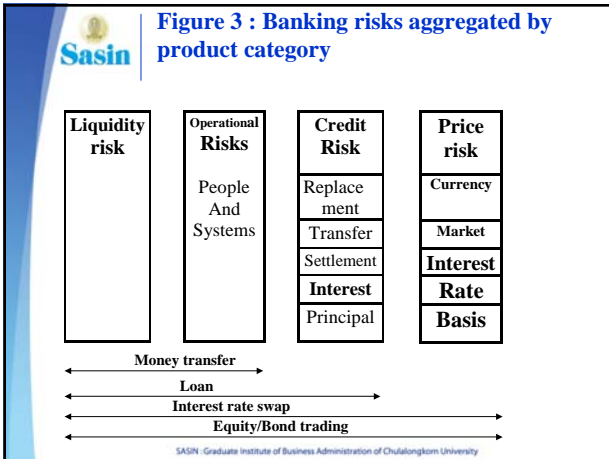
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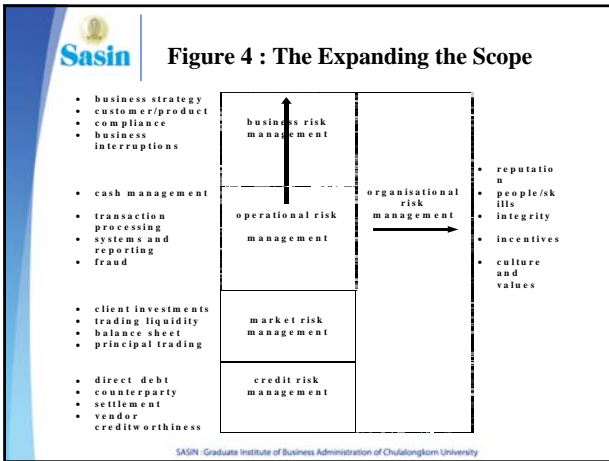


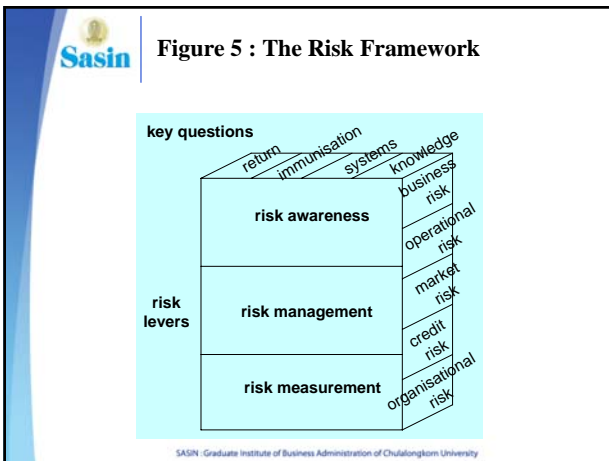
Non-trivial Categories of Risk

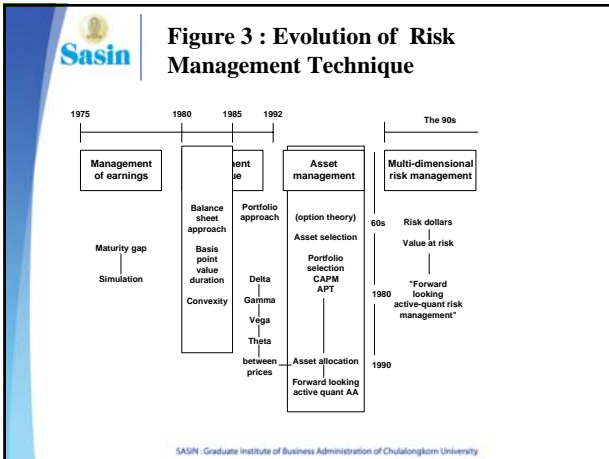
- 1) **Credit risk** : is possibly the most predominant risk of most commercial banks since unlike security firm, banks are asset sensitive due to imbedded options.
 - 2) **Market Risk** : or a systematic risk is the portion of a security's total risk that is related to moves in the market portfolio and ,hence, cannot be diversified away.
 - 3) **Liquidity Risk** : is, *for the market*, the price adversely response when the financial product is being liquidated.
For the own risk, the maximum of cumulative margin calls requiring cash payout in the time horizon (daily/intra day).
 - 4) **Systemic Risk** : is the interaction between different sources of risk. It is often called Correlation Risk.
- Note there is potential survivorship bias in estimating this risk.

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Evolution of Risk Management

I) Management of Earnings : (prior and in 1970's)

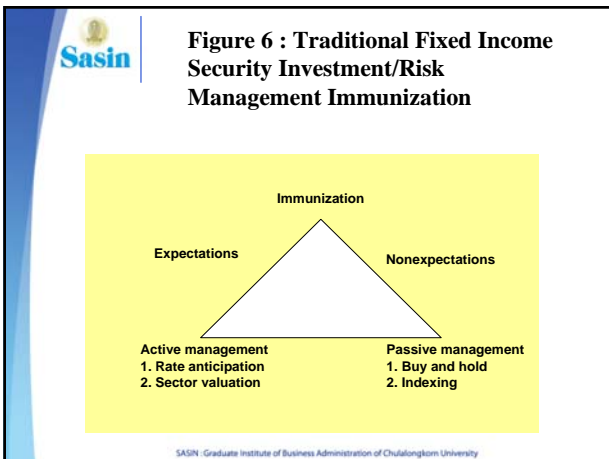
a) Maturity Gap : In *relatively stable* and *simple* balance sheet world, bank's liquidity or funding risk has been managed by using **accounting concept** - measuring the maturity mismatch, or gap, between asset and liabilities, but this provided *inadequate* measure of interest rate exposure.

In theory, a bank with a matched (Macaulay's) duration, or **zero gap**, between asset and liability portfolio will not experience a change in th market value of its asset/liability portfolio following an (incremental) interest rate change.

b) Simple 'Scenario/Simulation Analysis : This is a *forward looking* approach where the analyst examines how net income will *vary* in different interest rate and business activity environment under different shapes of the yield curve/spread.

c) Immunization Technique : In early 1950's, Redington developed immunisation tech. as a strategy by which one constructs and manages a portfolio of (component) bonds such that its value is always as close as possible to the value of another asset (the target). Note that the sources of total return depend on two things : 1) interest rate and 2) passage of time.

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Risk Management – (Time) Duration

e) Swap + Bond Duration : The combination portfolio is

$$D^P = \frac{1}{\sum W^B B_i + \sum W^S S_j} * (\sum W^B B_i D_i^B + \sum W^S B_j D_j^S) \quad (6)$$

f) Option Duration :

$$\frac{\delta Q}{\delta r} = \delta B \frac{\delta O}{\delta r} \quad \text{where } O = \text{call option on bond}$$

$B = \text{Market Price of the bond}$

$$\text{Delta} : \Delta = \delta \frac{Q}{B} \quad \text{by definition, so } \delta \frac{Q}{B} = \Delta \frac{\delta B}{\delta r} \quad (7)$$

From the definition of bond duration, (1) we rewrite

$$\delta \frac{Q}{B} = -\Delta B D^B \quad \text{then} \quad D^O = \Delta D^B \quad (8)$$

That is the duration of the option is simply the hedging delta ratio (i.e. the delta multiplied by the modified duration of the liability). Or we can rewrite

$$D^O = -\frac{1}{B} \frac{\delta Q}{\delta r} \quad \text{where } D^O = \text{Option Duration} \quad (9)$$

The portfolio duration for bond and option is

$$D^P = \frac{1}{\sum W^B B_i + \sum W^O O_j} * (\sum W^B B_i D_i^B + \sum W^O O_j D_j^O)$$

More Details and Derivation See Green [1996]



Risk Management – All that Greeks

II) Balance Sheet and Option Approach : (In 1980's)

a) Dollar Duration or Delta : is the potential volatility of the return from holding a particular bond.

$$-\Delta_s = \frac{\partial B}{\partial r} = \frac{\text{change in bond price}}{\text{change in int. rate in \%}}$$

b) Convexity or Gama : is the curvature of the performance profile at the current rate or price of the security.

$$\Gamma_s = \frac{\partial^2 B}{\partial r^2} = \frac{-\Delta_s}{\text{increase in the interest rate}}$$

c) Theta : provides a measure of the effect of the passage of time on the price of a particular bond.

$$\Theta = \frac{\partial B}{\partial t} = \frac{\text{change in bond price}}{\text{change in time}}$$

d) Vega : $\Lambda = \frac{\partial B}{\partial \sigma_r} = \frac{\text{change in bond price}}{\text{change in } r \text{ volatility}}$

Two General Comments :

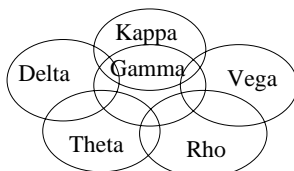
..All these Greeks are interrelated.

..Binomial Approach is commonly used for fixed income securities pricing and risk management.

[See more Vasicek 1977, Nelson and Ramaswamy 1990]



Figure 7 : Simultaneous Management of Risk Parameter – All that 'Greeks'



Sasin | Risk Management : Portfolio Approach

II) Portfolio Approach : (In 1980's) - Macro/Micro Econ

1. Capital Asset Pricing Model by Sharpe [1964, JF]

CAPM/SML : $E(R_i) = R_f + [E(R_m) - R_f] \beta_i$

Questions : What is it about the benchmark rate ?

- What is the risk free rate, R_f ?
- What is the Thai (sovereign) risk free rate, R_f^T ?
- What is the Thai (Baht) risk free rate, R_f^B ?
- What is the expected return of Thai Security, $E(R_i)$?
- What is the interest rate for Thai Corporate Bond, r^T ?
- What is Raroc ?

2. Option Pricing Model by Black and Scholes 1973 JPE : For the Equity and Bond Holder : As a Financial Contract.

Equity is a residual claim on firm's value with limited liability. The shareholders' wealth, S is

$$S = \text{Max.} [0, V - D]$$

Bond is a fixed claim on firm's value. The bondholders receive

$$B - P = \text{Min.} [V, D] \text{ for Risky Bond}$$

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Sasin | Risk Management – Portfolio Approach

3. Contemporaneous vs Intertemporal Risk Diversification

$$\sigma_i^2 = b_i^2 \sigma_m^2 + \sigma_{\epsilon_i}^2 \quad \text{where } b_i = \sigma_{im} / \sigma_m^2$$

Total risk = systematic risk + unsystematic risk

In theory, all unsystematic risks should be diversifiable.

What is about in practice in an incomplete (Arrow and Debreu sense) and imperfect world (MM spirit) ?

- Default Risk
- Bankruptcy cost
- Tax
- Legal Risk – Priority Claim ?
- Market Failures
- Agency Problem ...

4. Bond Covenants :

Sources of the Bondholder-Stockholder conflict :

- Restriction on Dividend Payment (23%)
- Restriction of Issuing New Debt (90%)
- Restriction on Merger Activity (39%)
- Restriction on the Disposition of the firm's Asset

5. Bond Rating Agencies

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Sasin | Risk Management – VaR Preview

II) Value at Risk (VaR) : (In 1990's)

a) VaR Key Concept

- VaR stands for Value at Risk.
- VaR is obtained by translating the market riskiness of any financial instruments into a common standard potential loss (one dimensional framework ?)
- VaR poses the primary question : How much money might we lose over the period of time ?
- VaR is a statistical estimate of how many dollars or bahts a firm risks losing over a specified period of time due to market price, a given a level of probability. (Critically assuming a normal distribution.)
- VaR is a method for measuring volatility-correlation sensitivity to factors affects the current position based on recent market volatility.
- VaR incorporates two main elements of risk
 - 1) Exposure amount of assets and liabilities in the portfolio.
 - 2) Sensitivity of the portfolio value due to the change of the underlying risk factors

- VaR's Main Applications : Info. Report, Resource Allocation, Performance Evaluation and Regulation.

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Risk Management – VaR Preview

b) The key issue : Integrating 'All' Risks.

A basic idea of VaR is to integrate all form of risk into a single summary number.

Because risk is a multi-dimensional entity, and several forms of nonlinearity and incompatibility exist, these conditions make risk integration quite difficult.

However, if we restrict our consideration to market price risk and suppose that such prices have a multivariate log/normal distribution, integration become analytically tractable.

More Generally , the Potential Loss =
 $\text{Volatility} * \text{Exposure} * \text{Timing} * \text{Correlation}$

J.P. Morgan – The 'Weatherstone Mandate – 4:15 Report' :

"At 4:15 p.m. every afternoon, I wish to receive a single number which summarizes the institution's total financial risk."

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Risk Management – VaR Concept

c) The VaR Concept : at Work

1. Value the current portfolio using today's price list. The components of this list will be called 'market factors'.
2. Revalue the current portfolio using an 'alternative price list' and calculate the change in the portfolio value.
3. Calculate the maximum the institution can lose over a specified 'time horizon' at a specified probability level.

The main problem is to find a series of vectors of 'alternative price list or market factors' to calculate VaR.

Three methods are used to calculate VaR :

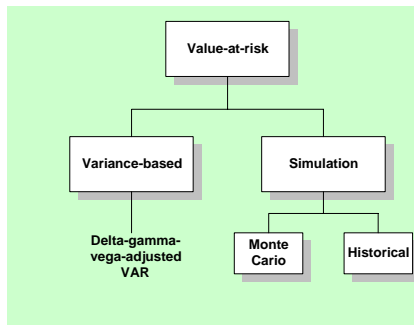
1. Historical method – fine with stationary world
2. Simulation method – good with potential event risks.
3. Analytic method – best for portfolios without options

Not surprisingly, the three methods deliver different VaR measures, particularly with the portfolio with options. Any Implications ?

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Figure 8 : Methods of estimating VaR



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VaR Preview : Historical method

Calculating VaR by the Historical Method – Backward Looking

1. Gather historical *volatilities* and *correlation* for financial variables. (Characterization!)
2. Specify a *model* for financial market. (Assumption !)
3. Using (1) and (2), construct a probability distribution for the loss/gain on the portfolio.
4. Your risk measure is then a single statistic that describes that distribution : Mean, Std. Deviation, confidence interval, etc.

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VaR Preview : Historical method (Cont.)

Example : Suppose that two asset portfolio is composed of
 a) 20 bonds with face value of \$1,000 and price at \$980 and
 b) 500 shares of a stock XYZ currently price at \$40.

The portfolio is at present worth \$ 39,600.

Suppose expected price change of the bond is 20 and of the stock is 5. The standard deviation of bond price change is 8.4 and of stock change is 82.30. The correlation is 0.2. Then,

$$E(\Delta V) = 20 E(\Delta B) + 500 E(\Delta S) = 20(20) + 500(5) = 2,900$$

$$(\sigma_v)^2 = (20)^2(8.4)^2 + (500)^2(8.4)^2 + 2(20)(500)(8.4)(82.3)(.2)$$

$$\sigma_v = 4,808$$

The VaR at the 95% level is \$5,033 = 1.65 (4,808) – 2,900

Similarly for a portfolio with K assets :

$$E(\Delta V) = \sum_k A_k E(\Delta P_k) ; (\sigma_v)^2 = \sum_k \sum_j A_k A_j \sigma_{PKPj} \rho_{k,j}$$

VaR = Loss at acceptable risk level (σ_v) – Expected (ΔV)

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Panel I : Historical Simulation VaR

Step 1: Revaluation of holdings for each day of preceding 250-day period on basis of historical prices (prices and values in dollars)

	Asset 1 (100,000 units)	Asset 2 (100,000 units)	Portfolio value		
	Price	Value	Price	Value	
Day 1	41	4.1m	30.2	3.02m	7.12m
Day 2	42	4.2m	30.8	3.08m	7.28m
Day 250	39.5	3.95m	30.0	3.0m	6.95m

Step 2: Sort values in ascending order

	Day	Portfolio value
1	Day 20	6.63m
2	Day 21	6.72m
3	Day 197	6.72m
12	Day 29	6.81m
249	Day 2	7.28m
250	Day 172	7.30m

Step 3: Choosing a confidence level of 5%, VaR is calculated by subtracting the 12th observation from the initial value of the portfolio (\$7m) :

$$VAR = \$7m - \$6.81m = \$0.19m$$

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VaR Preview : Simulation method

Calculating VaR by the Simulation method – Forward Looking

- a) Define the parameters of the distributions for the changes in market factors, including correlations among market factors.
- b) Specified distribution function (e.g. Normal, lognormal, etc.)
- c) Use the distributions in a Monte Carlo simulation to obtain possible market price outcomes and to observe changes in the market factors over the time horizon to be used.

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VaR Preview : Simulation method

$$\Delta NPV_t = \Delta NPV_{t+n} - \Delta NPV_t \text{ where } t = \text{begin date}$$

Note that Monte Carlo Simulation method – Direct Simulation of future distribution – *forward* looking.

But so-called ‘Historical Simulation’ methods – Correlation Matrix is a *backward* looking and (near) stationary assumpt.

Example : Risk of Portfolio is determined by Agg. Dist.

Date	-\$ Value	Dist.	-\$ Value	Dist.	Dist.
Day 1	300		304		
Day 2	297	+3	506		-2
Day 3	302	-5	506		0
Day 4	302	0	502		+4
Day 101	290	-6	456		-8
Risk Dollar	10,5		12		

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Multifactor VAR

Market factor focus

- Market value of each contract is described as a function of basic market rates
- Uncertain future market rates → Risk of fall in value

Step 1: Simulate changes in market factors

Simulation number	Simulated change in market factors			
	eg	Δ X1	Δ X2	Δ Xn
2	US\$/DM	1	US\$/JPY	US\$/P
3	—	—	—	SPOT WTI
4	—	—	—	—
5	—	—	—	—
NS	—	—	—	—

Step 2: Calculate resultant change in portfolio value

Simulated change in portfolio's market value	
ΔPV	
—	
—	
—	
—	
—	
—	

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VaR Preview : Analytic (Σ) method

Example : Suppose that a US portfolio manager holds a two-year, Deutschmark Bund with a face value of DM5,000 coupon, paid annually. Suppose further that the one-year and two year DM zero-coupon rates are 4.45% and 5.60% respectively, and the spot rate is DM1.45.

Mapping or Stripping a German Bund Cashflow



	DM/\$	1.0 yr	DM	2.0 yr	DM
DM Bund	\$3,444	\$182		\$3,262	

Given the Var-Cov Matrix for the three Bund Market Factor

	\$/DM	1yr DM zero	2yr DM zero
Dollar/D-Mark	1.85 E -5	-6.78 E -6	-3.50 E -6
One-yr D-Mark zero	-6.78 E -6	2.50 E -5	1.61 E -5
Two-yr D-Mark zero	-3.50 E -6	1.61 E -5	1.85 E -5

For the Deutschmark Bund, the portfolio variance is 348.57.

The standard deviation of the portfolio will be \$18.76.

A 95%, one day VaR will be 1.65 (\$18.67) = \$30.81

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VaR Preview : Pro and Con (14)

Advantage of VaR

- 1) Robust – summarizes broad spectrum risk with single number
- 2) Captures correlations and volatilities – hedging and diversification
- 3) Intuitively meaningful output :
The greater the risk, the higher VaR

Disadvantage of VaR

- 1) Does address only 'Business-as-usual' Risk
- 2) Assumes historical correlation will persist
- 3) Simple VaR models ignore Gamma/ Convexity Risk
- 4) All VaR models ignore out of the money gamma risk – Catastrophic Event Risk (Non-Statistical Solution ; Stress Testing, Back testing, What-if testing, Analyze crisis risk, Role of Liquidity, Price Discountinuity, etc.)

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Capital Adequacy Ration (CAR) and Var

The Building Block Approach

In April 1995, the Basle Committee on Banking Supervision, Bank of International Settlement (BIS) established the fundamental concept of CAR to distinguish between banking and trading books and to be effective in Jan '96. One alternative to accept CAR for market risk is called an *internal model based* approach as quantitative standards by using Var as follows :

$$\text{Market Risk Regulatory Capital} = \text{Max} [\text{VaR}_{\text{BIS}} (\text{today}), K * \text{VaR}_{\text{BIS}} (\text{60 day average})]$$

- a) Compiling daily
- b) Using a 99th percentile
- c) One-tailed confidence interval
- d) min. holding period 10 days
- e) Using observation of minimum one year
- f) An ave. of the daily VaR based on each of the preceding 60 business days.
- g) K = Multiplication factor. Normally set to 3.0.
[The actual K can be ranged from 3 to 4 based on 'back testing']

The capital at risk reserve will then become the higher of the previous day's Var multiplied by a factor (e.g. specific and general risks) assessed by each national supervisor.

For interest rate risk :

Specific Risk weighting rises from 0% for government debt in domestic currencies to 8% for non-qualifying items.

General Risk weighting ranging from 0 to 12.5% is based on a maturity or duration basis. The matched and unmatched positions are then multiplied by varying percentages to give the capital requirement.

See more Details on BIS [1993, 1996]

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Sasin | **Table 2 : Comparing of the Key Concept (d1)**

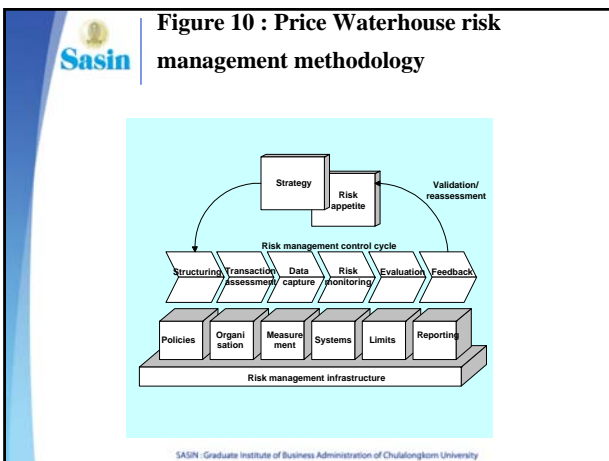
Quantitative Applications	
<i>Active Management</i> Return simulation	Predicts bond and portfolio behavior given alternative interest-rate scenario projections.
<i>Immunization</i> Immunization model	Creates and maintains a portfolio that will have an ensured return over a specified horizon, irrespective of interest-rate change.
<i>Passive Management</i> Indexing system	Creates and maintains a portfolio that will track the performance of a given bond index with a manageable set of securities.
<i>Individual Security Analysis</i> Swap systems	Allows for comparison of individual securities, with the objective of identifying historical price (or basis point spread) relationships.


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Sasin | **Table 2 : Comparing of the Key Concept (d2)**

Term-structure analysis	Evaluates the current level of yields by producing spot, discount, and forward-rate structures. Also values Treasury securities.
Bond valuation model	Develops a normative value for corporate and mortgage-backed securities, based on the evaluation of those characteristics of the security that contribute to overall price.
Contingent-claims model	Evaluates the embedded option in a security without forecasting interest rates.
<i>Other</i> Performance attribution system	Calculates the total return for a bond portfolio and attributes the return to its components.
Risk analysis report	Calculates option-adjusted average duration, convexity, and yield for a portfolio.

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END

see you next time
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